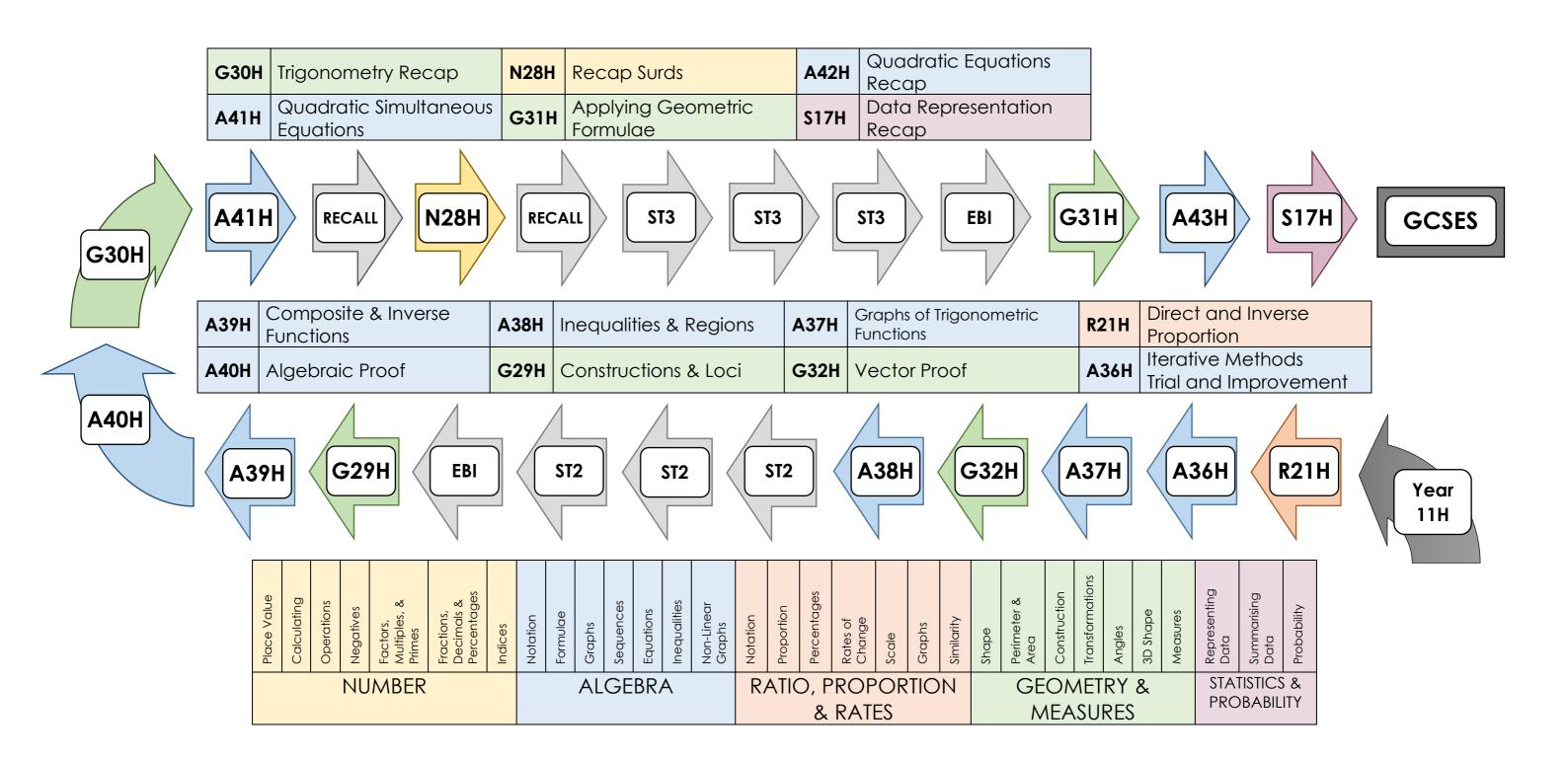
Strand		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
S E S E S E S E S E S E S E S E S E S E	Place Value		Place Value including decimals Rounding (all multiples) including 1 d.p.	Round to 1 significant figure for numbers greater than 1 Estimation (numbers greater than 1 only) Round to 2-3 significant figures	Significant figures including numbers less than 1 Estimate (including numbers less than 1) Error Intervals for powers of 10 Estimate more complex calculations	Error intervals from Calculations Significant figures including numbers less than 1 Estimate (including numbers less than 1)	Error intervals	TCUI 12	Rounding has been done since at least 2000 BCE Understanding the error implicit in a measurement, and how these errors can be compounded by further manipulation is key in both physical and statistical measurement.
		Add and subtract positive integers multiply THTU by TU Division using factors Long division Equivalent fractions & simplifying Fractions on a number line Compare and order fractions Add and subtract fractions Multiply fractions by integers Multiply fractions by integers Mixed calculations with fractions Fraction of an amount Reverse fraction of an amount Mult & div by 10, 100, 1000 Mult decimals by integers Divide decimals by integers	Four rules with decimals (multiply & divide by integers only)	Multiply & divide by multiples of powers of 10 Multiply decimals by decimals Add + subtract mixed number fractions (not improper)	Divide by decimals Use fraction, decimal equivalence to calculate efficiently Four rules with fractions	[Multi-step, interleave area &	Combo fraction [Multi-step, interleave area & perimeter]		Decimal fractions were first developed in China in the 4th Century BCE
	Calculating			Use fraction, decimal equivalence to calculate efficiently Order of operations (including squares	improper)	Fraction calculations in reverse Recap 4 rules Four rules with mixed numbers			Multi-base arithmetic reciprocals
	Operations		Order of operations Basic use of a calculator	order of operations (including squares and roots) Basic use of a calculator - use of fraction, square (root) keys Order of operations (Distributive property)	property) Use of fraction, index and negative keys Use calculator for standard form	(Embedded) Use of calculator Standard form calculations (simple cases)		Modelling	Precedence' is generally defined so that higher-level operations are performed first. The distributive law is one of the 9 Field axioms of mathematics, fundamental to how arithmetic; in all its forms,
	Negatives	Use negative numbers in context	Compare and order directed numbers	Multiply and divide with negatives Squaring negatives					Existence of additive inverse
	Factors, Multiples and Primes	Common tactors	Division facts Squares and roots Identify factors, multiple and primes by lisiting	HCF & LCM by listing HCF & LCM in context	Prime Factors (calc and non-calc) Identify factors from prime factor form	HCF & LCM with prime factors (using a	Recap Surds		Transerable into fractions, algebraic manipulation, proof
	actions, Decimals		Convert between fractions, decimals,	Convert between improper fractions and mixed numbers Compare, and order lists of; fractions, decimals, and percentages (simple cases) Convert between improper fractions	Convert between fractions, decimals, and percentages (including calculator use) Compare, and order lists of; fractions, decimals, and percentages				Ancient Egyptians could calculate with fractions, though they only used fractions with numerators of 1 (the multiplicative inverses) Proof of limits of series may rely on understanding the effect of multiplying fractions, as does combining
s 	Frai M Prai		Index notation	Index Laws (not fractional, negative) Write a number as a power of a base [e.g. 64 = 48]	decimals, and percentages >100% Index Laws (inc negative)	Index laws for fractional indices standard form add/sub (4 ops) lindex Laws negative powers Change of base [8² = 4³] Standard Form			probabilities.

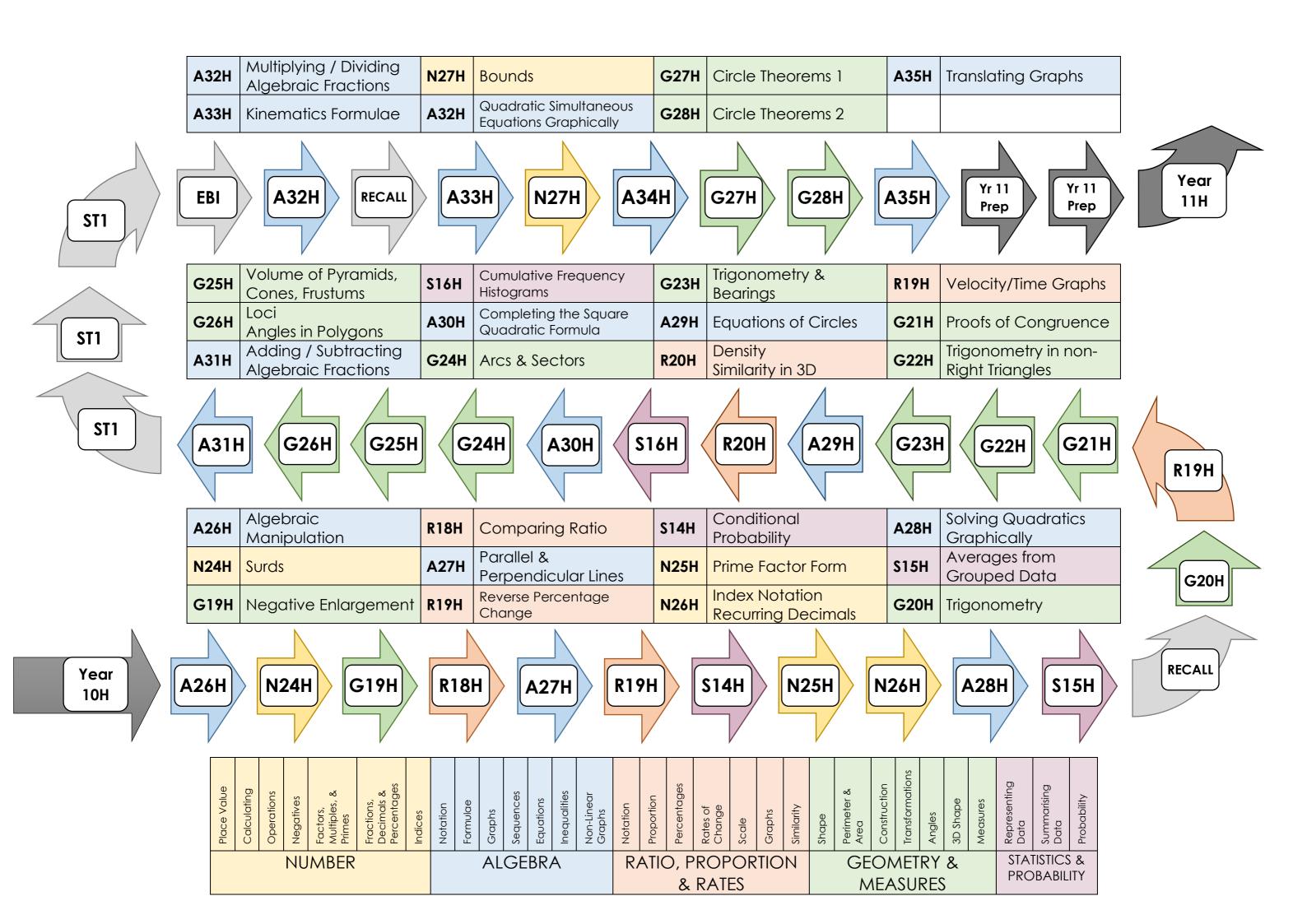
Strand		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale	
S	Notation			Expand brackets Factorise to one bracket (number factor) Algebraic index laws Factorise to one bracket (algebraic factor)	Expand two added brackets and simplify Factorise to one bracket Algebraic index laws Expand two subtracted brackets and simplify	Expand pairs of brackets a>1 factorise quadratics a>1 Expand 3 brackets Complete the square Turning points - translate graphs of quads Alg fractions: simplify add/subtract multiply/divide Simplify alg fractions [(4x + 6)/2] Expand two subtracted brackets and simplify Expand pairs of brackets (a=1) Factorise quadratics (a=1)			Persian mathematician al- the 8 th Century. The word of derives from the islamic wo	Algebra was brought to Europe by Persian mathematician al-Kwarizmi in the 8 th Century. The word algebra derives from the islamic word al-jabr which means "reunion of broken parts"
S	Formulae	The state of the s	Form formulae from contexts	Substitute into complex formulae (Powers and roots) Change the subject (2 & 3 step)	Substitute into complex formulae [use kinematics formulae] Change subject involving powers and roots	Change subject involving factorising	Change the subject involving factorising		Ancient Greek and Babylonian mathematicians wrote formulas as sentences. As symbolic algebra developed (mainly in the Arab world) it eventually found favour in Europe and was used by Rene Decartes to show that geometric problems could be solved by using algebra (he also popularised the use of x as the unknown). As formulas often model real world situations it can be helpful to rearrange them so that the term to be calculated is the subject.	
Algebra	Graphs		y=x & y= -x [referring to patterns in coordinates]	Solve equations graphically (intersect with x=a, y=a)	Plot ax + by = c Equation of a line from two points Solve linear simultaneous equations graphically	Perpendicular lines Solve quadratics graphically Solve sim eq linear and quadratic graphically Draw a line to solve a quadratic Translate graphs Plot ax + by = c Equation of a line from two points Equations of parallel lines Solve linear simultaneous equations graphically		Proof Sequences & Series Functions Parametric Equations Trigonometric Functions Further Algebra Trigonometric Identites Differential Equations Numerical Analysis Polynomials	The method of graphing functions can be extended to two variables, three dimensions, and even the complex plane in illustrating many areas of mathematics, including the Riemann hypothesis, the 'Holy Grail' of mathematical proof.	
	Sequences		term rule	Describe using nth term Relate nth terms to patterns	Quadratic sequences [n²+c] Nth term of geometric sequence (simple cases)	Quadratic sequences [an²+bn+c] Quadratic sequences [n²+c] Nth term of geometric sequence (simple cases)		Moments Projectile Motion Modelling Friction	Mathematicians work with the sums of sequences, called series and is a major part of calculus. This has led to proofs about infinite sums	
S	Equations	Form equations from word problems Solve 1 and 2 step equations Pairs of values for multi-variable equations	Solve equations [linear, 1 & 2 step, (inc 10 - 2x = 4)] Form equations	Solve equations [linear, 1 & 2 step, 1 bracket] Form equations Solve equations [inc fractions with numerical denominators]	Solve equations [inc brackets, fractions with numerical denominators] Solve equations with unknowns on both sides Solve linear simultaneous equations without scalling Solve equations with unknowns and brackets on both sides Solve linear simultaneous equations where one must be scaled		Composite functions Inverse functions Trial and improvement Iteration Sim Eq w/ quadratic Factorise and solve quadratic equations (a=1) Linear simultaneous equations (link to graphs)		The equals sign was invented in 1557 by Welsh mathematician Robert Recorde who said that "nothing can be more equal than two parallel lines of equal length"	
S	Inequalifies		Notation Represent on a number line not compound)	CONTRACTOR OF THE PARTY OF THE	Solve linear inequalities (2 step, inc compound) Represent inequalities on a coordinate plane	Solve 2 variable linear inequalities algebraically Combining regions Solve compound Two variable inequalities [list sets of solutions] Regions for single inequalities	Solve 1 variable quadratic inequalities algebraically Solve inequalities graphically		Mathematicians often use inequalities to bound quantities for which exact formulas cannot be computed easily. Some inequalities are used so often that they have names.	
S	on- near raphs			Plot simple quadratics Plot simple quadratics	Plot simple quadratics & cubics Find approximate solutions	Equation of circles transform graphs	y = a^x trig graphs Plot cubics, y=a^x Recognise non-linear forms		6	
	Z 3 0			Find approximate solutions	Plot y = ax2+bx+c	Speed from distance-time graphs	sketch filling curves			

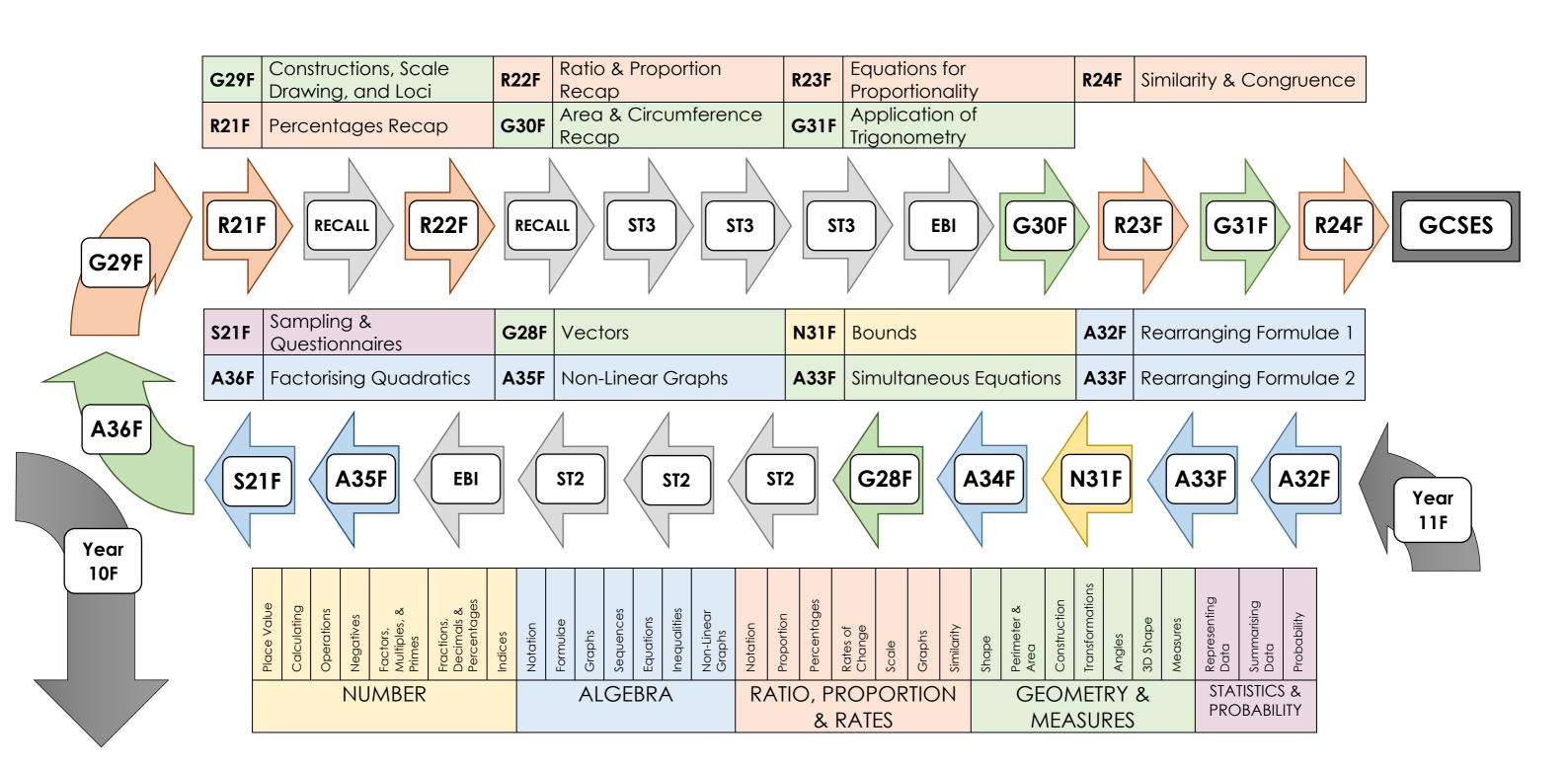
Strand		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
ınge	ation	Use ratio notation	Use ratio notation & simplify Relate ratios to fractions	Share in a given ratio Unit ratio	Solve ratio division where one part is known Divide into 3 part ratio	combo ratio combo questions Solve ratio division where one part or			It was thought that all numbers could be written as ratios (and, in fact, an infinite number are). We now know that there are an infinite number of irrational numbers that cannot be.
Cho	S To N		Scaling (recipes) Equivalence of ratio	Share in a given ratio (inc dec ans) Best buy by scaling Solve simple direct proportion problems	Solve ratio division where one part or difference is known Best buy by unit ratio Solve simple direct or inverse proportion problems	difference is known Divide into 3 part ratio Solve inverse proportion problems	Write inverse proportion formulae Solve proportion problems involving 3 variables		
o f (Proportion			Solve simple direct or inverse proportion problems	Write direct (inc squares, roots) proportion formulae	3 part ratio [m:f,f:c,m:c] combo ratio algebraic & graphically	Write direct and inverse proportion formulae (x and x²)		In ancient Rome a tax of 1/100 of
Rates	S	Percentage of amounts without a calculator Reverse percentage of amount	Percentage of amounts without a	One number as a percentage of another Compare proportions using percentage Calculate percentages of amounts with a multiplier	Reverse percentage of an amount [40% of a number is 60, what is the number?] Percentage change with a multiplier Percentage profit/loss	Reverse percentage change with a multiplier Percentage profit/loss (with repeated percentage change) Consecutive % change [+25% then + 20%, etc] Simple interest		Proof Sequences & Series Functions Parametric Equations	every sale at auction was introduced. As denominations of currency grew throughout the Middle Ages, the ability to easily measure 1/100th of an amount (and multiples thereof) became more useful, and led to the decimalisation of most of Europe between the 17th and 18th Centuries.
~ ~	Thercentage			Percentage change with a multiplier	Consecutive % change [+25% then + 20%, etc]	Reverse percentage change with / without a multiplier Percentage profit/loss (with repeated percentage change) Tax		Trigonometric Functions Further Algebra Trigonometric Identites Differential Equations Numerical Analysis	
.o	s of		Calculate speed in simple cases [Within Distance-Time graphs]	Calculate speed/distance/time	Calculate speed/distance/time in more complex cases (i.e. multiples of 12 mins)	Compound Measures (Density, Pressure) Dimensional Analysis Convert compound measures		Moments Projectile Motion Modelling Friction	
	Scale Chan			Calculate speed/distance/time with multiples of 15 minutes Scale drawing	Calculate with other rates of change/ compound measures Map scales	[metres/min to Km/hr] {embed in speed unit}	Compound measures (Density, within Volume unit)		
odo.				[1cm = 5m etc] {embed in construction} Harder scale drawing [2cm = 5m etc] {embed in construction}	[1:50:000] {embed in loci, bearings} Harder map scales [1:125:000] {embed in loci, bearings}				
), Pr	s		Plot and interpret (piece-wise linear) distance-time graphs	Graphs of direct proportion [Use to solve]	Graphs of direct proportion [Use to solve, find gradient and relate to context]	Velocity-time graphs [rate of change, trapezium rule, average speed] Calculate gradients to tangents of curves and interpret in context.	Inverse proportion graphs		
atic	Graphs			Graphs of direct proportion [Use to solve, find gradient and relate to context]	Graphs of inverse proportion	Graphs of direct proportion [inc. squares]			The understanding of rate of change links with acceleration, gradient of a line, conversion rates etc. Graphs of rate of change can be analysed using calculus.
22	Simil Simil					Area and Volume scale factors Find lengths/scale factor			

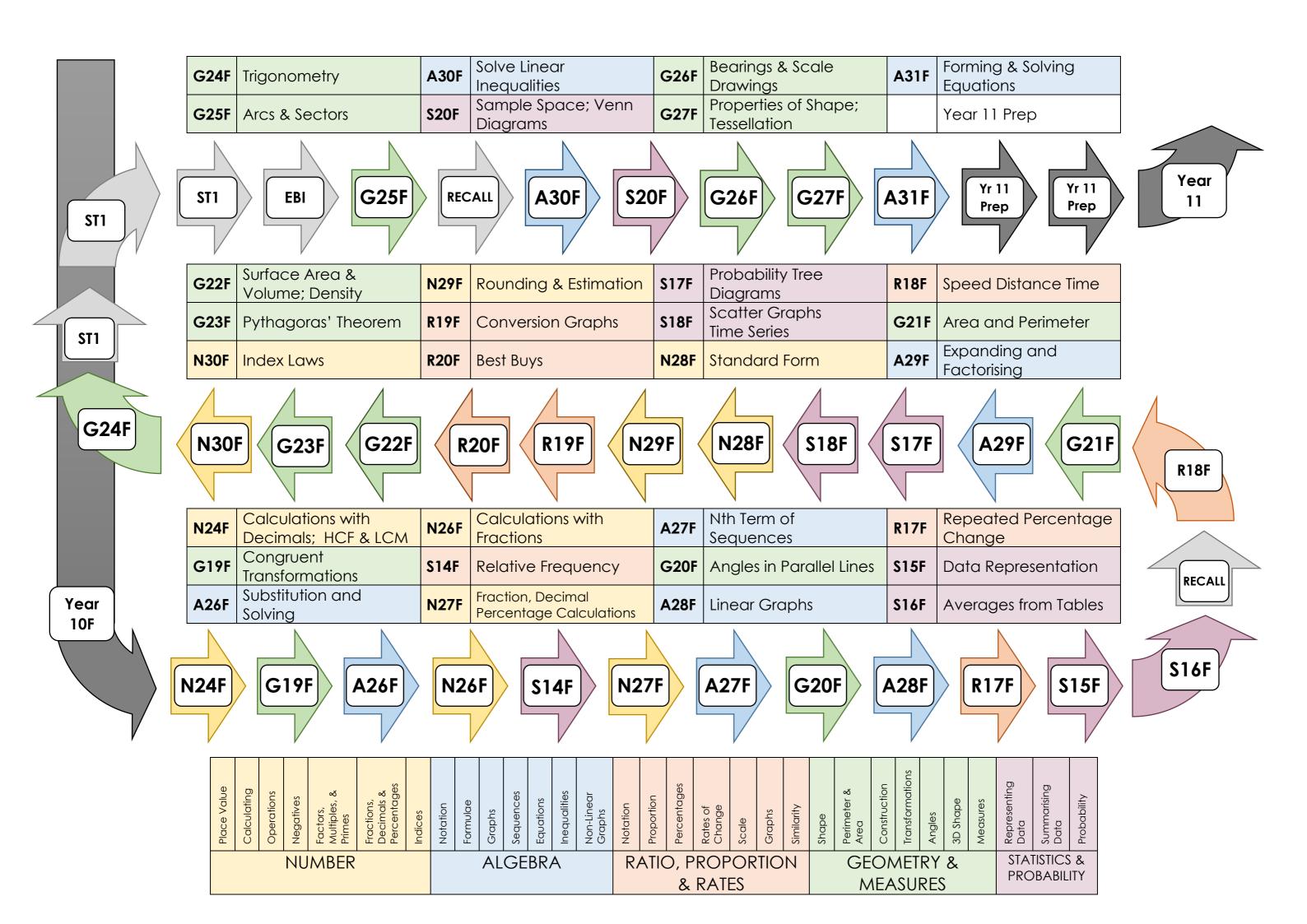
Strand		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
S	ape	_	Properties of triangles/quadrilaterals (inc symmetry) Parts of the circle	Properties of quadrilaterals (inc symmetry) Parts of the circle (all)	Pythagoras	I3D Pythag 3D Trig Non RA Trig Pythagoras & bearings	Non calc Trig Applications of Trigonmetry [bearings, circle theorems etc.] Non calc Trig		Classification Projective geometry Topology
	She		Area of parallelogram, triangle, trapezium	Classifying quadrilaterals	3D Pythagoras	Trigonometry (Right angled only)	, and a sub-		
	eter & Are	Perimeter and area of rectilinear	Area and perimeter of rectilinear shapes	Circumference and area of circles Area of compound shapes (not circles)	Arcs & Sectors (easy fractions of turn)	Reverse arc & sector (find angle) area of segment	Applications of area formulae		Calculating area is a key application of integral calculus, which can be
, E	Perim				Arcs & Sectors (other fractions of turn)	Arcs & Sectors			transferred to functions in higher dimensions, probability density theory, and kinematics. These techniques are a key step in
es es	noi		Triangle construction including SSS	Scale Drawing Recall standard constructions Loci	Combinations of Loci		Review inc scale, bearings		understanding Euclidean Geometry (c. 200 BCE), which is the foundation upon which all modern mathematics
\s\r	Construct	mangle constructions ASA and SAS		Construct 90°, 45°, 60°, 30° etc	Construction, congruence and proof	Bearings	Construction, scale drawing, combinations of Loci Similarity, congruence (reference enlargement)		
<u> </u>		Reflection over axes Translation (no vector notation) Enlarge by positive integer sf (no centre)	Reflect (horiz and vert only) Rotate		Describe reflections & rotations Enlarge (inc Fractional enlargement)	Transformations inc. negative enlargement	Magnitude of a vector Vector proof [using ratio, prove parallel, etc]	Trigonometry Vectors	
Seometry & M	Transformation			Enlarge (inc Fractional enlargement)	Combine translations (Vector addition)	Enlarge including fractional Combinations of transformations Combine translations (Vector addition)	Vector addition, multiplication by a scalar Represent a 2-dimensional vector and draw olumn vectors on a square or coordinate grid.		The ideas of transforming shapes on a plane can be extended into higher dimensions. Matrices are often introduced through their ability to perform transformations
		Measure and draw Angle facts Angles in a triangle Angles in a quadrilateral Angles in polygons	Notation Angle facts Angles in triangle, quadrilateral, angle properties Exterior angles of reg polygons	tiangle sum is 180°)	Int angles of polygons Angle proof (congruence, similarity)	Circle theorems			360° was chosen to be the number of degrees (parts) of a full turn by the Babylonians in around 1000 BCE. Other angle measurement systems include radians and gradians, which break the full turn up into different sized degrees. Geometric proots were some of the
	Angles			Back bearings Plans & elevations	Angle proof inc Isosceles triangles in circles	Int angles of polygons Angle proof (congruence, similarity)			earliest to be formulated, introducing the concept of abstract proof and mathematics as a discipline. Angles can be used to visualise complex numbers in the field of complex analysis.
s		Volume of cuboids Nets of prisms	Names (+ faces, edges, vertices) Volume of prisms Construct shapes from nets	Draw isometric	Surface area of prisms Volume of cylinders	Cones, spheres, frustums, pyramids	Applications of volume formulae		Calculating volume by considering
Ē	3D Shape				DONE Vol cylinders SA + Volume of pyramids	Surface area of cylinders Surface Area and Volume of Spheres, Cones, Pyramids and Composite solids Plans & Elevations			small slices was key in the development of integral calculus, which can be transferred to functions in higher dimensions, probability density theory, and kinematics.
S	Measures	Calculate with metric measures	Convert metric measures Calculate with time and timetables	Convert between metric area	Convert between metric area and volume				Atter the French Revolution (1789-99) the opportunity arose for a completely new measurement system. The French Academy of Sciences decided that
		Miles and kilometres Metric & Imperial measures		Solve problems involving area unit conversion	Solve problems involving volume unit conversion	See Ratio, Proportion and Rates of Change			

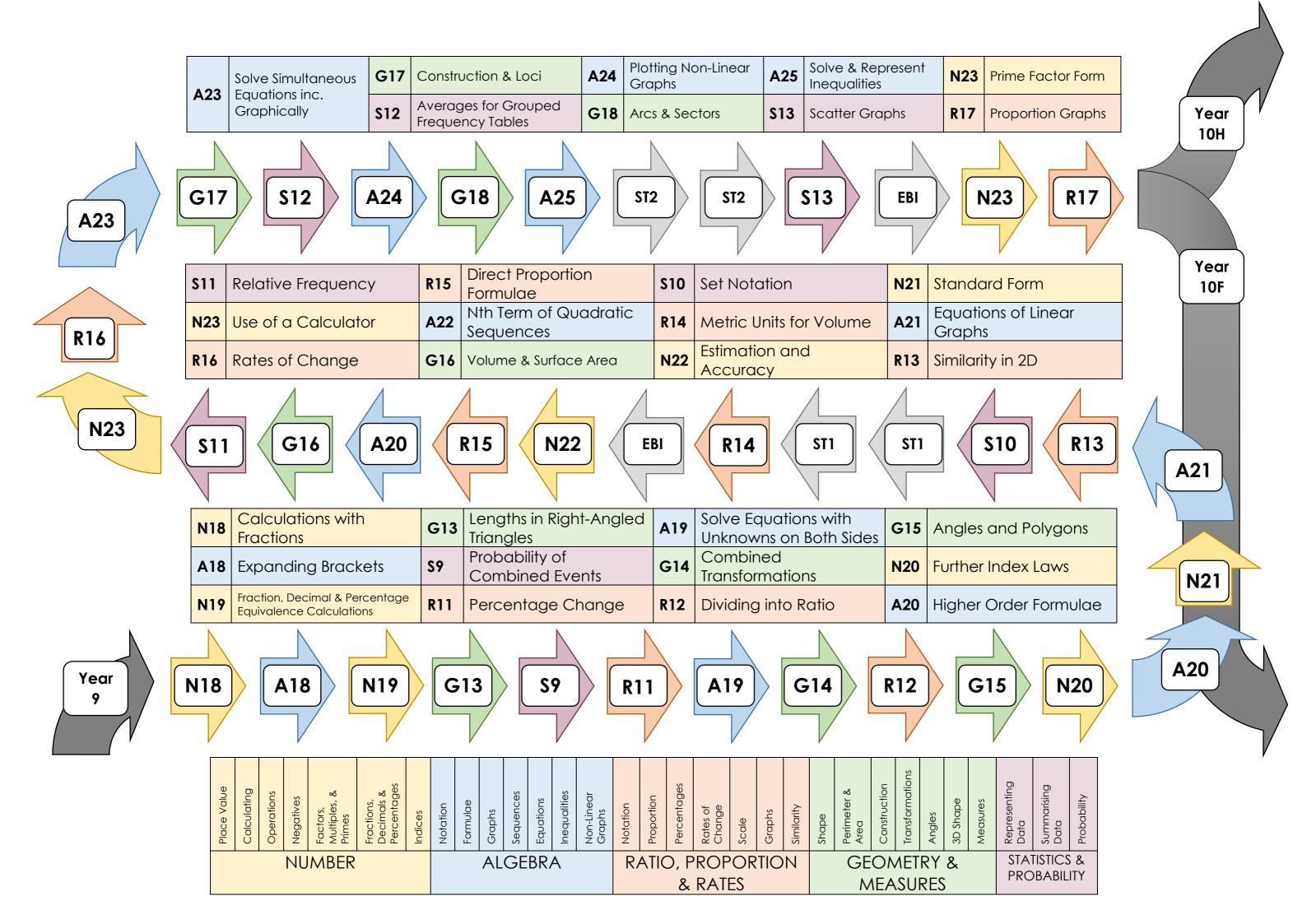
Strand		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
ty	S		Bar charts [compound and comparitive] Time series	Frequency diagram Frequency polygon Pie charts	Scattergraphs Stem & Leaf	Histograms Box plots	Recap of data	ecap of data	
babilit	Representing	Time series Read and interpret pie charts		Calculating quantities from pie charts		Scattergraphs	Misleading graphs, sampling bias and questionnaires		Data visualisations have the power to communicate information clearly. However, they can also be manipulated to mislead. Understanding time series graphs helps students to understand the concepts of rate of change, which in turn introduces kinematics, financial rates and derivative calculus.
& Pro	S		Probability scale Probability as a fraction (inc sum to 1) Listing outcomes complete probability space	Two-way tables Venn diagrams Experimental [find P(outcome) from experiment]	Frequency trees Probability tree diagrams [independent only] Set notation inc shading Relative frequency [use past data to make	Probability trees (inc dependent) Venn probability [P out of a subset, not a whole]		Conditional Probability Statistical Distributions Statistical Hypothesis Testing Staistical Sampling	Understanding probability was perhaps initially driven by games of chance, but also has been used in cryptography and cryptanalysis since the 8th century.
S	Probability			Judge bias	Comparisons with expected values	Prequency frees Probability tree diagrams [independent only] Set notation inc shading Relative frequency [use past data to make predictions] Relative frequency graphs Judge bias		staistical sampling	Now used in risk assessment and modelling, in particular in finance, but also in medicine, behavioural science and biology. It is key to understanding quantum theory.
Statisti	Describing	Mean Mean from frequency table	Averages and range collect data in frequency table Mode from frequency table	Complete data knowing averages Mean from frequency table Median from freq table	Complete grouped frequency Estimate mean from grouped frequency Identify group containing median	Interpret cumulative frequency graph (top 10% pass, etc) Compare data sets using box plots Problem solve with averages Median from freq table	Recap Data Handling		The arithmetic mean was developed by astronomers in the 16th Century, knowing that variance in their records was more likely to be errors in measurement than the moon changing size.











	G12 Bearings & Scale Drawing	A17 Plotting Quadratics	N16 Indices A16 Solve Linear Inequalities
	R10 Direct Proportion Graphs	R9 Converting Units for Area	N17 Multiplying Decimals N15 HCF & LCM
Year 9	R10 G12 R9	A17 N17 N1	16 N15 A16 R8 EBI R7 A15
	\$8 Averages from Tables	G11 Translation &	A15 Changing the Subject S9 Experimental Probability
	A13 Expanding and Factorising	A14 Solving Equations	G12 Representing 3D Shapes R7 Direct Proportion Problems ST2
	G10 Constructions and Loci	N13 Mixed Numbers	N14 Calculating with Fractions R8 Speed. Distance, Time
R6	G8 S8 EBI	A13 G10 G1	1 A14 N13 A15 G12 N14 S9
	A12 Substitution with Negatives	S7 Two-Way Tables and Venn Diagrams	A10 Nth term of a Sequence N9 Use of a Calculator
EBI	R6 Sharing in Ratio	N11 Rounding and Estimation	S6 Representing Continuous Data N10 Order of Operations
	G8 Angles in Parallel Lines	R5 Percentages and Finance	A11 Equation of a Straight Line G7 Area and Circumference of Circles
A12	ST1 ST1 R5	N11 S7 A1	S6 A10 G7 N10 N9 Year 8
	Place Value Calculating Operations Negatives Factors, Multiples, & Primes Fractions, Decimals & Percentages	Notation Formulae Graphs Sequences Inequalities Non-Linear Graphs Notation	Percentages Rates of Change Scale Scale Graphs Angles Angles Angles Angles Angles Angles Angles Angles Perimeter & Area Construction Transformations Angles Bepresenting Data Probability
	NUMBER	ALGEBRA RAT	GEOMETRY & STATISTICS & PROBABILITY & RATES MEASURES STATISTICS & PROBABILITY

