





# Algebra

		Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
S	Notation	Form expressions	Vocabulary [expression, term, rule, etc] Form expressions (no division) Simplify by collecting terms (no negative answers)	Expand brackets Factorise to one bracket (number factor) Algebraic index laws	Expand two added brackets and simplify Factorise to one bracket Algebraic index laws	Expand pairs of brackets $a>1$ factorise quadratics $a>1$ Expand 3 brackets Complete the square Turning points - translate graphs of quads Alg fractions: simplify add/subtract multiply/divide		Proof Sequences & Series Functions Parametric Equations Trigonometric Functions Further Algebra Trigonometric Identities Differential Equations Numerical Analysis Polynomials Moments Projectile Motion Modelling Friction	Algebra was brought to Europe by Persian mathematician al-Kwarizmi in the 8 <sup>th</sup> Century. The word algebra derives from the islamic word <i>al-jabr</i> which means "reunion of broken parts"
E					Factorise to one bracket (algebraic factor)	Expand two subtracted brackets and simplify	Simplify alg fractions [(4x + 6)/2] Expand two subtracted brackets and simplify Expand pairs of brackets (a=1) Factorise quadratics (a=1)		
S	Formulae	Use function machines Substitute into expressions Use formulae	Substitute into simpler formulae Form formulae from contexts Change the subject (1 & 2 step)	Substitute into complex formulae (Powers and roots) Change the subject (2 & 3 step)	Substitute into complex formulae [use kinematics formulae]	Change subject involving factorising			Ancient Greek and Babylonian mathematicians wrote formulas as sentences. As symbolic algebra developed (mainly in the Arab world) it eventually found favour in Europe and was used by Rene Decartes to show that geometric problems could be solved by using algebra (he also popularised the use of x as the unknown).
E									Change subject involving powers and roots
S	Graphs	Plot coordinates in all four quadrants	Plot horizontal and vertical lines, $y=x$ & $y=-x$ [referring to patterns in coordinates] Plot $y=Mx+C$ using table of values	Solve equations graphically (intersect with $x=a$ , $y=a$ ) Gradient & Intercept Equation of a line (pos int gradient)	Plot $ax + by = c$ Equation of a line from two points Solve linear simultaneous equations graphically	Perpendicular lines Solve quadratics graphically Solve sim eq linear and quadratic graphically Draw a line to solve a quadratic Translate graphs			
E									Equation of a line (neg. frac. gradients)
S	Sequences		Generate sequences from term-to-term rule Generate sequences from position-to-term rule Describe patterns with sequences inc triangular and square	Describe using nth term Relate nth terms to patterns Describe and continue geometric sequences and the fibonacci sequence	Quadratic sequences $[n^2 + c]$	Quadratic sequences $[an^2+bn+c]$			
E									Describe and continue fibonacci-type sequences
S	Equations	Form equations from word problems Solve 1 and 2 step equations Pairs of values for multi-variable equations	Solve equations [linear, 1 & 2 step, (inc $10 - 2x = 4$ )] Form equations	Solve equations [linear, 1 & 2 step, 1 bracket] Form equations	Solve equations [inc brackets, fractions with numerical denominators] Solve equations with unknowns on both sides Solve linear simultaneous equations without scaling	Solve quadratics using the formula	Composite functions Inverse functions Trial and improvement Iteration Sim Eq w/ quadratic		The equals sign was invented in 1557 by Welsh mathematician Robert Recorde who said that "nothing can be more equal than two parallel lines of equal length"
E									
S	Inequalities		Notation Represent on a number line not compound)	Solve linear inequalities (1 step, not compound) Represent on a number line (inc compound)	Solve linear inequalities (2 step, inc compound)	Solve 2 variable linear inequalities algebraically Combining regions	Solve 1 variable quadratic inequalities algebraically Solve inequalities graphically		
E									Solve linear inequalities (2 step, inc compound)
S	Non-Linear Graphs			Plot simple quadratics	Plot simple quadratics & cubics Find approximate solutions	Equation of circles transform graphs	$y = a^x$ trig graphs		
E									Plot simple quadratics Find approximate solutions



Strand			Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale	
Ratio, Proportion, & Rates of Change	S	Notation	Use ratio notation	Use ratio notation & simplify Relate ratios to fractions	Share in a given ratio Unit ratio	Solve ratio division where one part is known Divide into 3 part ratio	combo ratio combo questions		Proof Sequences & Series Functions Parametric Equations Trigonometric Functions Further Algebra Trigonometric Identites Differential Equations Numerical Analysis Moments Projectile Motion Modelling Friction	It was thought that all numbers could be written as ratios (and, in fact, an infinite number are). We now know that there are an infinite number of <i>irrational</i> numbers that cannot be.	
	E				Share in a given ratio (inc dec ans)	Solve ratio division where one part or difference is known Divide into 3 part ratio	Solve ratio division where one part or difference is known Divide into 3 part ratio				
	S	Proportion		Scaling (recipes) Equivalence of ratio	Best buy by scaling Solve simple direct proportion problems	Best buy by unit ratio Solve simple direct or inverse proportion problems		Write inverse proportion formulae Solve proportion problems involving 3 variables			
	E				Solve simple direct or inverse proportion problems	Write direct (inc squares, roots) proportion formulae	Solve inverse proportion problems 3 part ratio [m : f, f : c, m : c] combo ratio algebraic & graphically	Write direct and inverse proportion formulae (x and x²)			
	S	Percentage	Percentage of amounts without a calculator Reverse percentage of amount	Percentage of amounts without a calculator Percentage increase/decrease non-calculator	One number as a percentage of another Compare proportions using percentage Calculate percentages of amounts with a multiplier	Reverse percentage of an amount [40% of a number is 60, what is the number?] Percentage change with a multiplier Percentage profit/loss	Reverse percentage change with a multiplier Percentage profit/loss (with repeated percentage change) Consecutive % change [+25% then + 20%, etc] Simple interest			In ancient Rome a tax of 1/100 of every sale at auction was introduced. As denominations of currency grew throughout the Middle Ages, the ability to easily measure 1/100th of an amount (and multiples thereof) became more useful, and led to the decimalisation of most of Europe between the 17th and 18th Centuries.	
	E										
	S	Rates of Change		Calculate speed in simple cases [Within Distance-Time graphs]	Calculate speed/distance/time	Calculate speed/distance/time in more complex cases (i.e. multiples of 12 mins)	Compound Measures (Density, Pressure) Dimensional Analysis				
	E										Calculate speed/distance/time with multiples of 15 minutes
	S	Scale			Scale drawing [1cm = 5m etc] {embed in construction}	Map scales [1 : 50 000] {embed in loci, bearings}					
	E										Harder scale drawing [2cm = 5m etc] {embed in construction}
	S	Graphs		Plot and interpret (piece-wise linear) distance-time graphs	Graphs of direct proportion [Use to solve]	Graphs of direct proportion [Use to solve, find gradient and relate to context]	Velocity-time graphs [rate of change, trapezium rule, average speed] Calculate gradients to tangents of curves and interpret in context.	Inverse proportion graphs			
	E										Graphs of direct proportion [Use to solve, find gradient and relate to context]
	S	Similarity					Area and Volume scale factors				
	E										Find lengths/scale factor

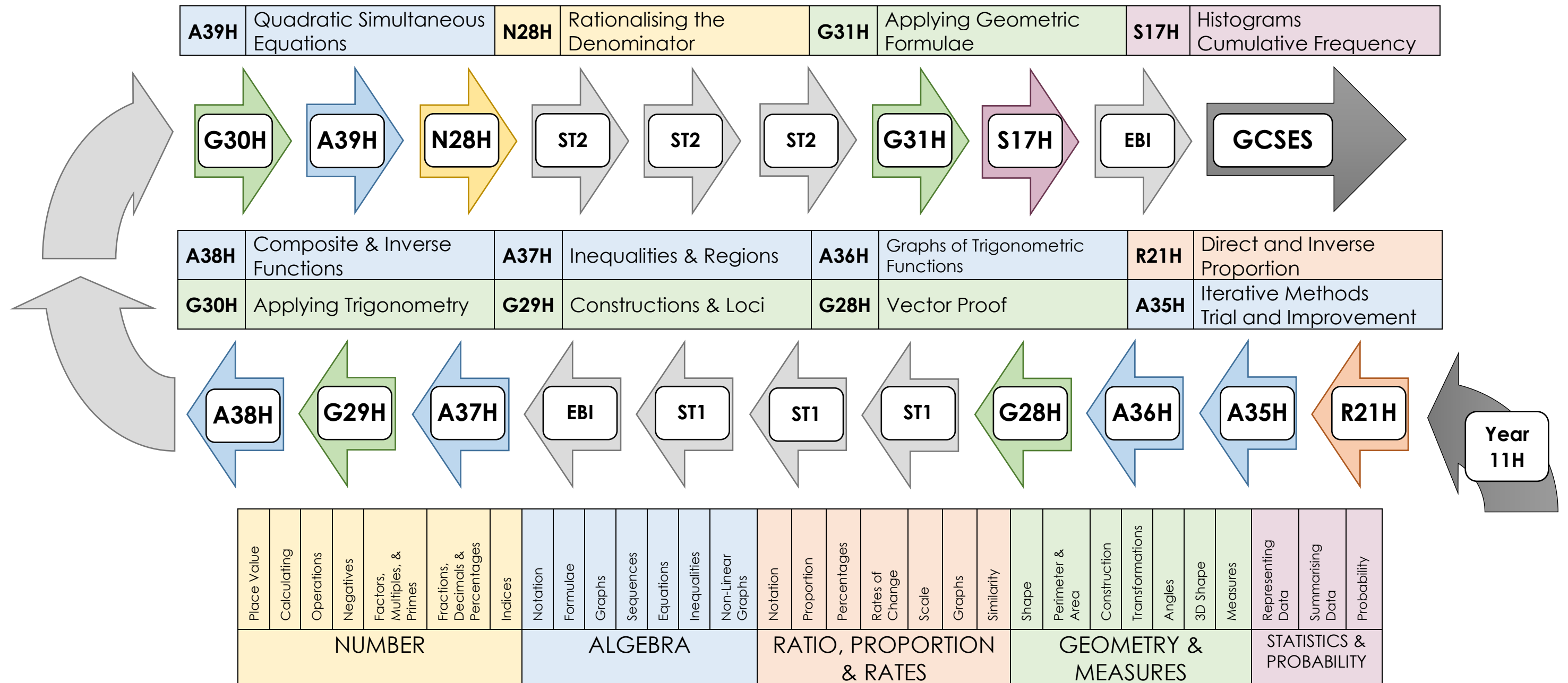


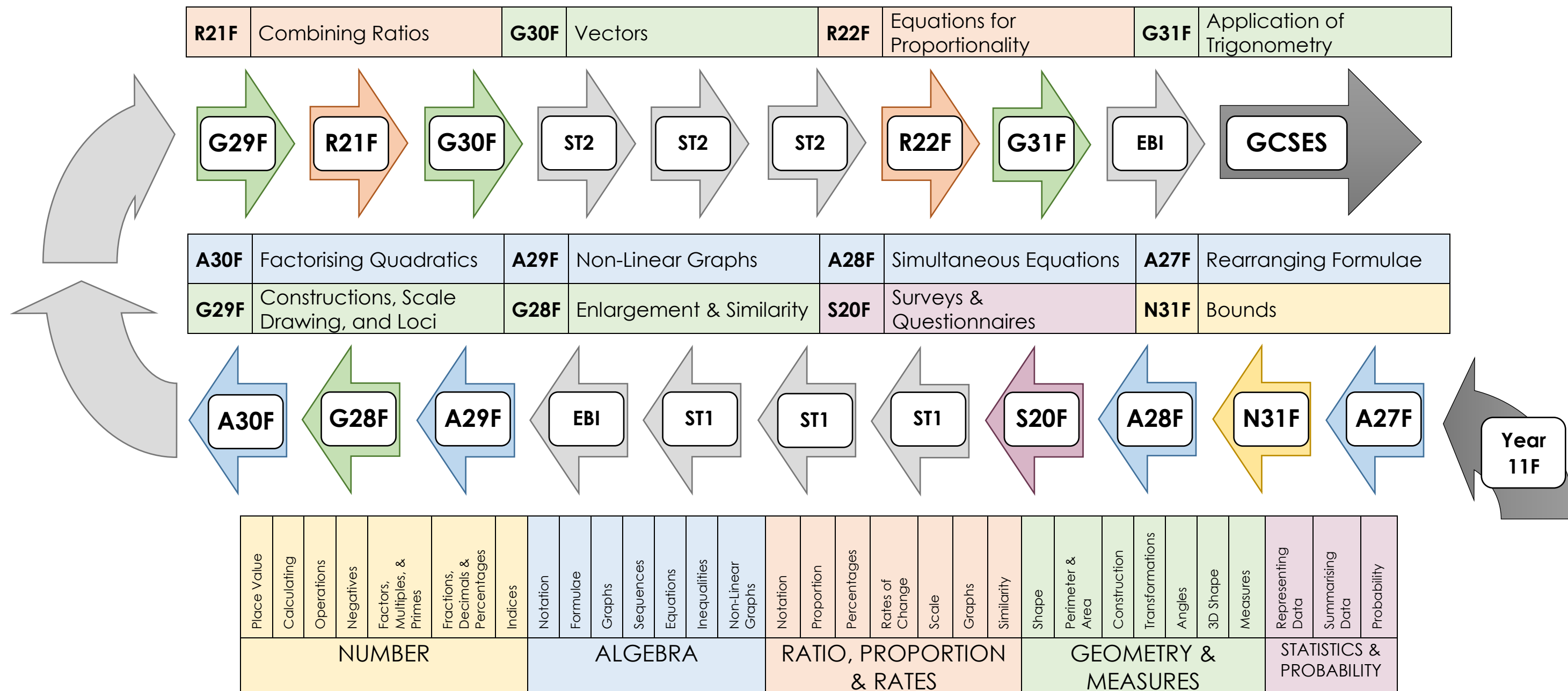
Geometry & Measures

Strand			Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
Geometry & Measures	S	Shape	Parts of the circle	Properties of triangles/quadrilaterals (inc symmetry) Parts of the circle	Properties of quadrilaterals (inc symmetry) Parts of the circle (all)	Pythagoras	3D Pythag 3D Trig Non RA Trig	Non calc Trig Applications of Trigonometry [bearings, circle theorems etc.]	Trigonometry Vectors	Classification Projective geometry Topology
	E				Classifying quadrilaterals		3D Pythagoras	Pythagoras & bearings Trigonometry (Right angled only)		Non calc Trig
	S	Perimeter & Area	Perimeter and area of rectilinear shapes Area of a triangle Area of a parallelogram	Area of parallelogram, triangle, trapezium Area and perimeter of rectilinear shapes	Circumference and area of circles Area of compound shapes (not circles)	Arcs & Sectors (easy fractions of turn)	Reverse arc & sector (find angle) area of segment	Applications of area formulae		
	E				Area of compound shapes (inc circles)		Arcs & Sectors (other fractions of turn)			Arcs & Sectors
	S	Construction	Triangle constructions ASA and SAS	Triangle construction including SSS Standard constructions	Scale Drawing Recall standard constructions Loci	Combinations of Loci		Review inc scale, bearings		These techniques are a key step in understanding Euclidean Geometry (c. 200 BCE), which is the foundation upon which all modern mathematics
	E				Construct 90°, 45°, 60°, 30° etc		Construction, congruence and proof	Bearings		Construction, scale drawing, combinations of Loci Similarity, congruence (reference enlargement)
	S	Transformation	Reflection over axes Translation (no vector notation) Enlarge by positive integer sf (no centre)	Reflect (horiz and vert only) Rotate	Translate Scaling translations Enlarge (pos int sf only)	Describe reflections & rotations Enlarge (inc Fractional enlargement)	Transformations inc. negative enlargement	Magnitude of a vector Vector proof [using ratio, prove parallel, etc]		
	E				Enlarge (inc Fractional enlargement)		Combine translations (Vector addition)	Enlarge including fractional Combinations of transformations Combine translations (Vector addition)		Vector addition, multiplication by a scalar Represent a 2-dimensional vector and draw olumn vectors on a square or coordinate grid.
	S	Angles	Measure and draw Angle facts Angles in a triangle Angles in a quadrilateral Angles in polygons	Notation Angle facts Angles in triangle, quadrilateral, angle properties Exterior angles of reg polygons	Angles in parallel lines (inc proof triangle sum is 180°) Draw and calculate bearings	Int angles of polygons Angle proof (congruence, similarity)	Circle theorems			360° was chosen to be the number of degrees (parts) of a full turn by the Babylonians in around 1000 BCE. Other angle measurement systems include radians and gradians, which break the full turn up into different sized degrees.
	E				Back bearings		Int angles of polygons Angle proof (congruence, similarity)			Geometric proofs were some of the earliest to be formulated, introducing the concept of abstract proof and mathematics as a discipline. Angles can be used to visualise complex numbers in the field of complex analysis.
	S	3D Shape	Volume of cuboids Nets of prisms	Names (+ faces, edges, vertices) Volume of prisms Construct shapes from nets	Plans & elevations Draw isometric Construct shapes from nets	Nets of 3D shapes Surface area of prisms Volume of cylinders	Cones, spheres, frustums, pyramids	Applications of volume formulae		
	E					DONE Vol cylinders SA + Volume of pyramids	Surface area of cylinders Surface Area and Volume of Spheres, Cones, Pyramids and Composite solids Plans & Elevations	Calculating volume by considering small slices was key in the development of integral calculus, which can be transferred to functions in higher dimensions, probability density theory, and kinematics.		
	S	Measures	Convert metric measures Calculate with metric measures Miles and kilometres Metric & Imperial measures	Convert metric measures Calculate with time and timetables	Convert between metric area	Convert between metric area and volume				After the French Revolution (1789-99) the opportunity arose for a completely new measurement system. The French Academy of Sciences decided that
	E				Solve problems involving area unit conversion	Solve problems involving volume unit conversion	See Ratio, Proportion and Rates of Change			



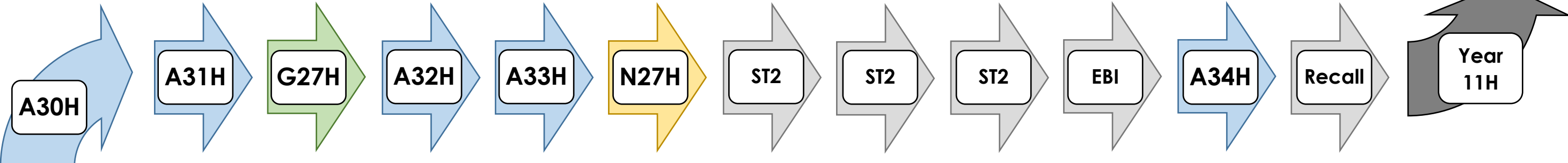
Strand			Year 6	Year 7	Year 8	Year 9	Year 10	Year 11	Year 12	Rationale
Statistics & Probability	S	Representing	Time series Read and interpret pie charts	Bar charts [compound and comparative] Time series Timetables	Frequency diagram Frequency polygon Pie charts	Scattergraphs Stem & Leaf	Histograms Box plots	Recap of data	Conditional Probability Statistical Distributions Statistical Hypothesis Testing Staistical Sampling	
	E									Data visualisations have the power to communicate information clearly. However, they can also be manipulated to mislead. Understanding time series graphs helps students to understand the concepts of rate of change, which in turn introduces kinematics, financial rates and derivative calculus.
	S	Probability		Probability scale Probability as a fraction (inc sum to 1) Listing outcomes complete probability space	Two-way tables Venn diagrams Experimental [find P(outcome) from experiment]	Frequency trees Probability tree diagrams [independent only] Set notation inc shading Relative frequency [use past data to make	Probability trees (inc dependent) Venn probability [P out of a subset, not a whole]			Understanding probability was perhaps initially driven by games of chance, but also has been used in cryptography and cryptanalysis since the 8th century.
	E									
	S		Mean Mean from frequency table	Averages and range collect data in frequency table Mode from frequency table	Complete data knowing averages Mean from frequency table	Complete grouped frequency Estimate mean from grouped frequency	Interpret cumulative frequency graph (top 10% pass, etc) Compare data sets using box plots Problem solve with averages			The arithmetic mean was developed by astronomers in the 16th Century, knowing that variance in their records was more likely to be errors in measurement than the moon changing size.
	E	Describing			Median from freq table	Identify group containing median	Median from freq table	Recap Data Handling		
					Calculating quantities from pie charts	Cumulative Frequency	Scattergraphs	Misleading graphs, sampling bias and questionnaires		



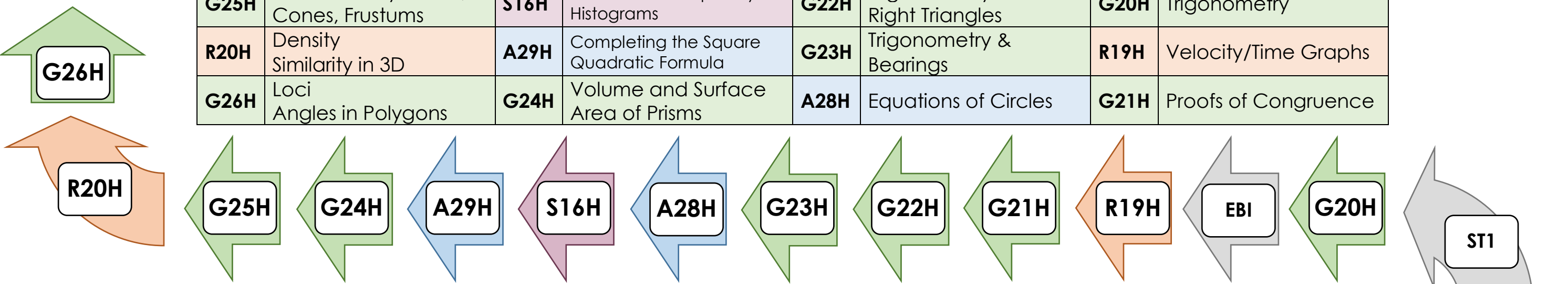




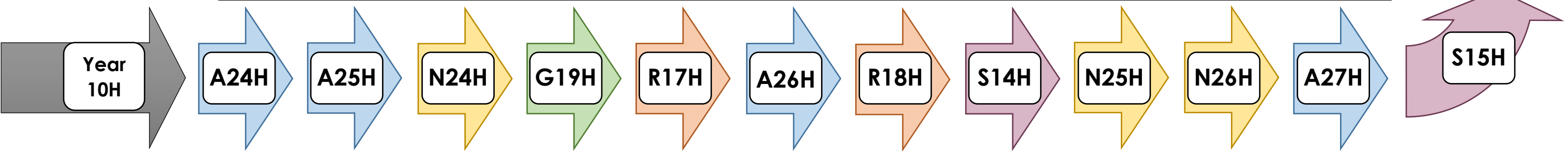
<b>A30H</b>	Adding / Subtracting Algebraic Fractions	<b>G27H</b>	Circle Theorems	<b>A33H</b>	Quadratic Simultaneous Equations by Substitution	<b>A34H</b>	Translating Graphs
<b>A31H</b>	Multiplying / Dividing Algebraic Fractions	<b>A32H</b>	Quadratic Simultaneous Equations Graphically	<b>N27H</b>	Bounds		



<b>G25H</b>	Volume of Pyramids, Cones, Frustums	<b>S16H</b>	Cumulative Frequency Histograms	<b>G22H</b>	Trigonometry in non-Right Triangles	<b>G20H</b>	Trigonometry
<b>R20H</b>	Density Similarity in 3D	<b>A29H</b>	Completing the Square Quadratic Formula	<b>G23H</b>	Trigonometry & Bearings	<b>R19H</b>	Velocity/Time Graphs
<b>G26H</b>	Loci Angles in Polygons	<b>G24H</b>	Volume and Surface Area of Prisms	<b>A28H</b>	Equations of Circles	<b>G21H</b>	Proofs of Congruence



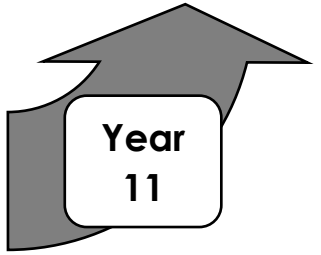
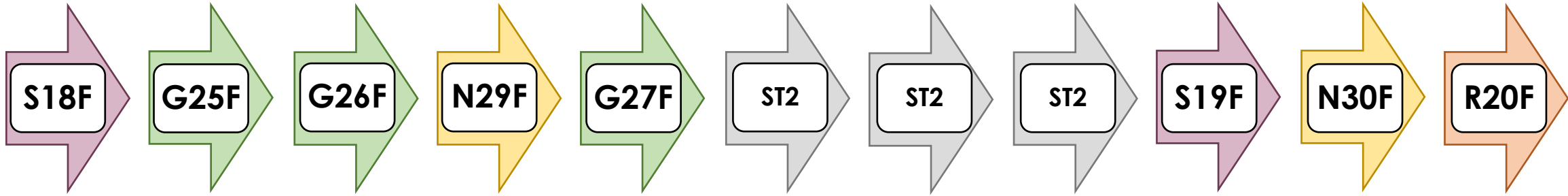
<b>A24H</b>	Factorising Quadratics	<b>G19H</b>	Negative Enlargement	<b>R18H</b>	Reverse Percentage Change	<b>N26H</b>	Index Notation Recurring Decimals
<b>A25H</b>	Rearranging Formulae	<b>R17H</b>	Comparing Ratio	<b>S14H</b>	Conditional Probability	<b>A27H</b>	Solving Quadratics Graphically
<b>N24H</b>	Surds	<b>A26H</b>	Parallel & Perpendicular Lines	<b>N25H</b>	Prime Factor Form	<b>S15H</b>	Averages from Grouped Data



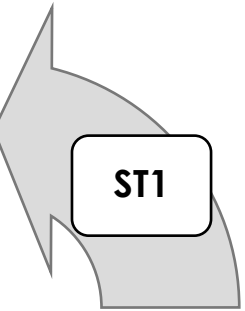
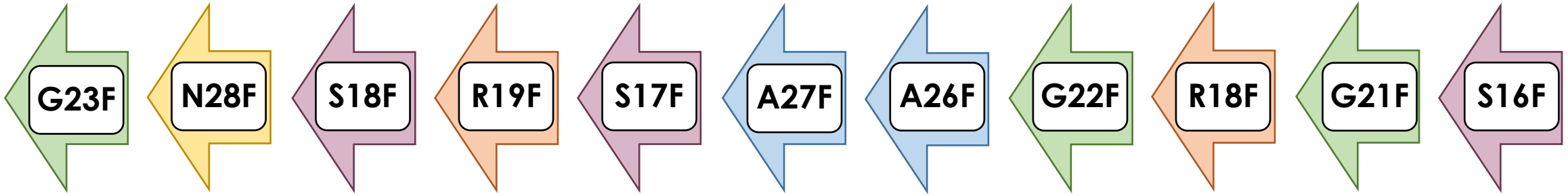
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NUMBER							ALGEBRA							RATIO, PROPORTION & RATES							GEOMETRY & MEASURES							STATISTICS & PROBABILITY		



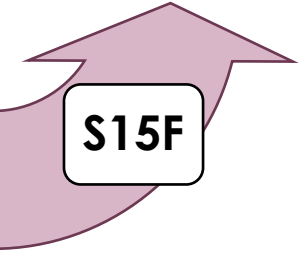
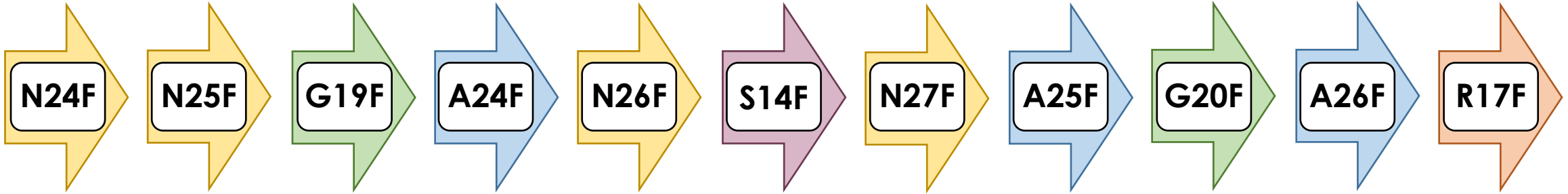
<b>G25F</b>	Surface Area, Volume, Density	<b>N29F</b>	Index Laws	<b>S19F</b>	Probability Tree Diagrams	<b>R20F</b>	Best Buys
<b>G26F</b>	Arcs & Sectors	<b>G27F</b>	Trigonometry	<b>N30F</b>	Standard Form		



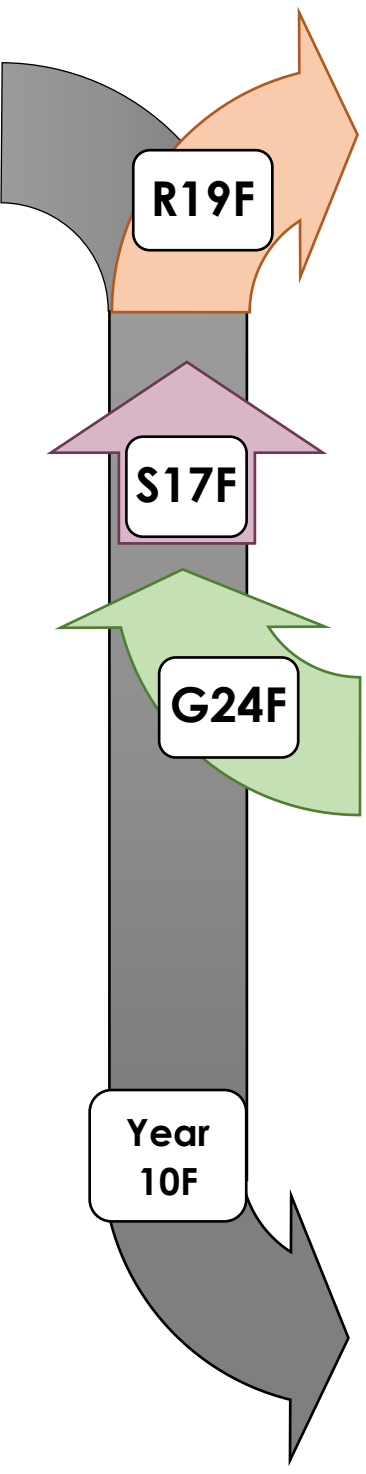
<b>N28F</b>	Rounding & Estimation	<b>S17F</b>	Scatter Graphs Time Series	<b>G22F</b>	Area & Perimeter in Context	<b>S16F</b>	Averages from Tables
<b>G23F</b>	Bearings	<b>R19F</b>	Conversion Graphs	<b>A26F</b>	Expanding and Factorising	<b>G21F</b>	Tessellation Plans & Elevations
<b>G24F</b>	Lengths of Right-Angled Triangles	<b>S18F</b>	Sample Space Venn Diagrams	<b>A27F</b>	Solve Inequalities	<b>R18F</b>	Speed Distance Time



<b>N24F</b>	Calculations with Decimals	<b>A24F</b>	Substitution and Solving	<b>N27F</b>	Fraction, Decimal Percentage Calculations	<b>A26F</b>	Linear Graphs
<b>N25F</b>	HCF & LCM Using Prime Factors	<b>N26F</b>	Calculations with Fractions	<b>A25F</b>	Nth Term of Sequences	<b>R17F</b>	Repeated Percentage Change
<b>G19F</b>	Congruent Transformations	<b>S14F</b>	Relative Frequency	<b>G20F</b>	Angle Proof	<b>S15F</b>	Data Representation

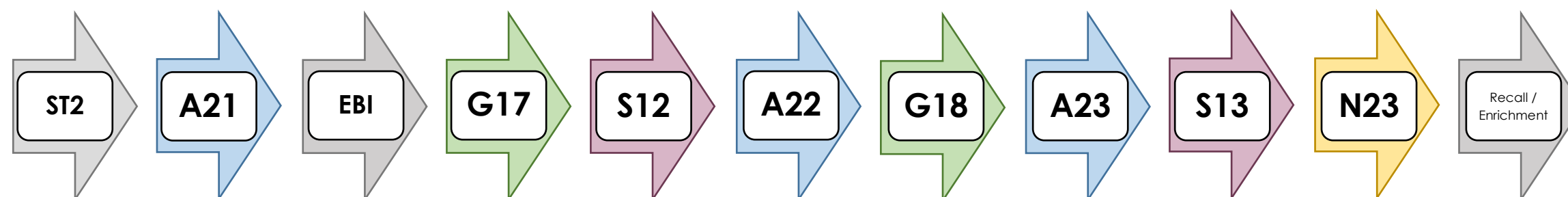


Place Value	Calculating	Operations	Negatives	Factors, Multiples, & Primes	Fractions, Decimals & Percentages	Indices	Notation	Formulae	Graphs	Sequences	Equations	Inequalities	Non-Linear Graphs	Notation	Proportion	Percentages	Rates of Change	Scale	Graphs	Similarity	Shape	Perimeter & Area	Construction	Transformations	Angles	3D Shape	Measures	Representing Data	Summarising Data	Probability
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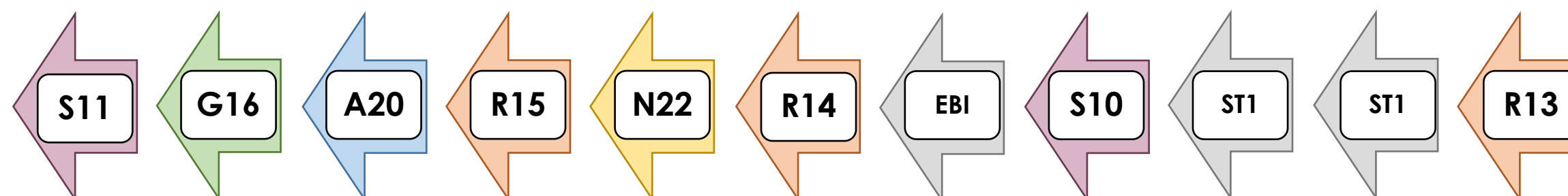




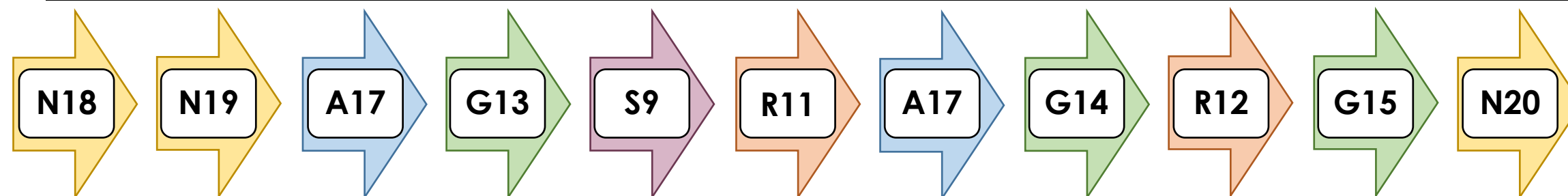
<b>A21</b>	Solve Simultaneous Equations inc. Graphically	<b>S12</b>	Averages for Grouped Frequency Tables	<b>G18</b>	Arcs & Sectors	<b>S13</b>	Scatter Graphs & Stem-and-Leaf
<b>G17</b>	Construction & Loci	<b>A22</b>	Plotting Non-Linear Graphs	<b>A23</b>	Solve & Represent Inequalities	<b>N23</b>	Prime Factor Form



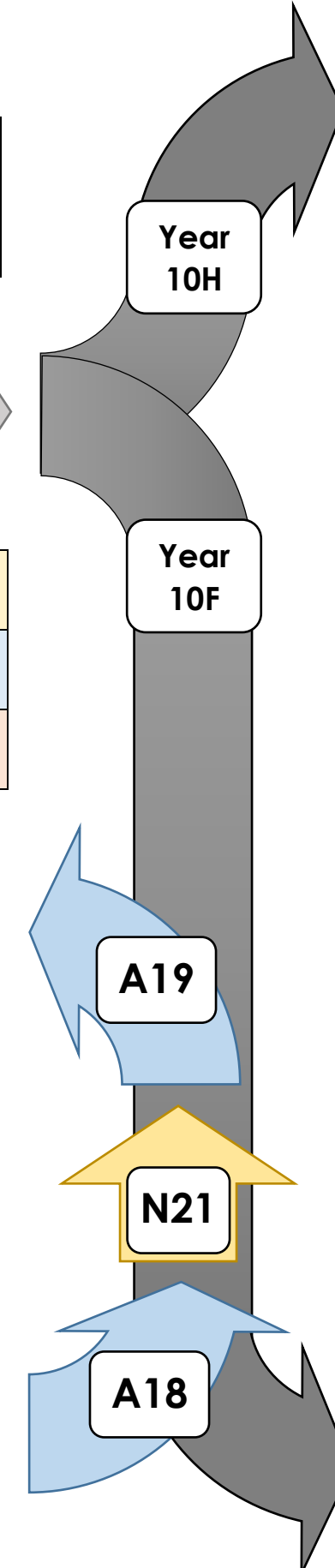
<b>S11</b>	Relative Frequency	<b>R15</b>	Direct Proportion Formulae	<b>S10</b>	Set Notation	<b>N21</b>	Standard Form
<b>N23</b>	Use of a Calculator	<b>A20</b>	Nth Term of Quadratic Sequences	<b>R14</b>	Metric Units for Volume	<b>A19</b>	Equations of Linear Graphs
<b>R16</b>	Rates of Change	<b>G16</b>	Volume & Surface Area	<b>N22</b>	Estimation and Accuracy	<b>R13</b>	Similarity in 2D



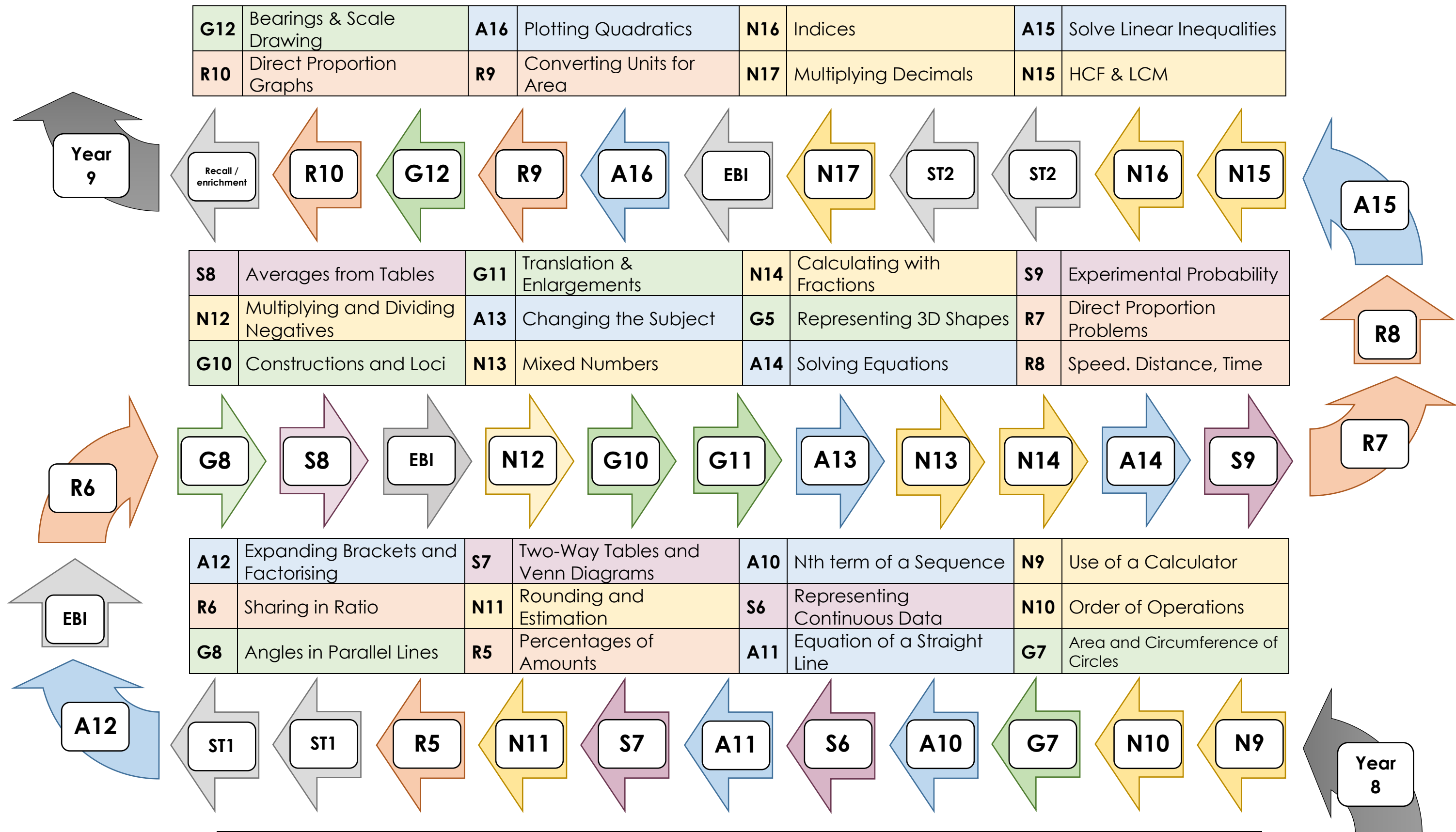
<b>N18</b>	Calculations with Fractions	<b>G13</b>	Lengths in Right-Angled Triangles	<b>A17</b>	Higher Order Formulae	<b>G15</b>	Angles and Polygons
<b>N19</b>	Fraction, Decimal & Percentage Equivalence Calculations	<b>S9</b>	Probability of Combined Events	<b>G14</b>	Combined Transformations	<b>N20</b>	Further Index Laws
<b>A17</b>	Expanding Brackets	<b>R11</b>	Percentage Change	<b>R12</b>	Dividing into Ratio	<b>A18</b>	Solve Equations with Unknowns on Both Sides



Place Value	Calculating	Operations	Negatives	Factors, Multiples, & Primes	Fractions, Decimals & Percentages	Indices	Notation	Formulae	Graphs	Sequences	Equations	Inequalities	Non-Linear Graphs	Notation	Proportion	Percentages	Rates of Change	Scale	Graphs	Similarity	Shape	Perimeter & Area	Construction	Transformations	Angles	3D Shape	Measures	Representing Data	Summarising Data	Probability
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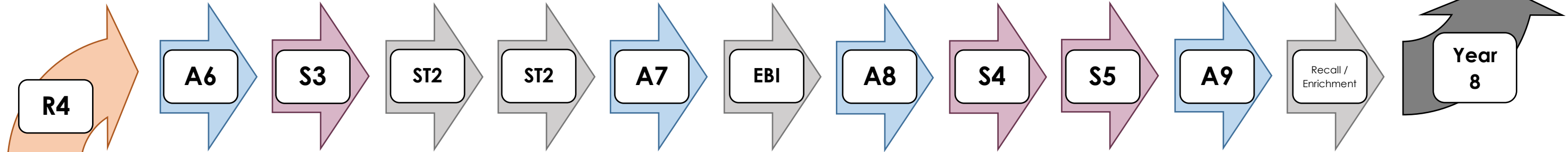




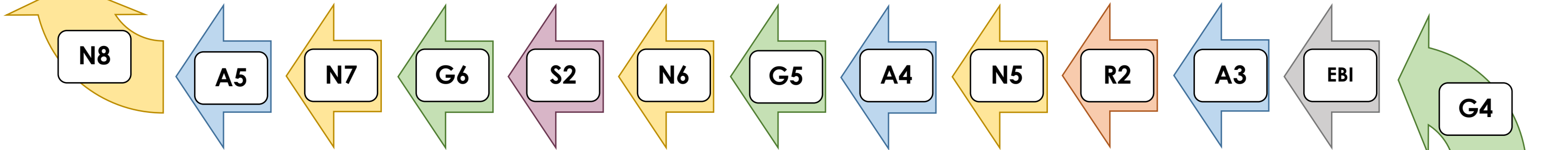




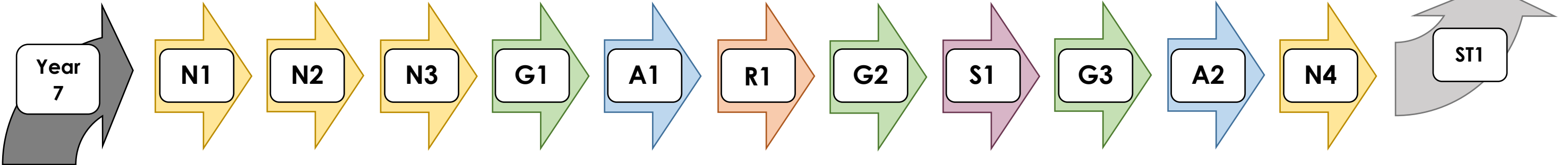
<b>R4</b>	Percentages with a Multiplier	<b>S3</b>	Averages for Small Data Sets	<b>A8</b>	Plot Linear Functions	<b>S5</b>	Time Series Graphs
<b>A6</b>	Changing the Subject of a Formula	<b>A7</b>	Representing Inequalities	<b>S4</b>	Tables & Timetables	<b>A9</b>	Distance-Time Graphs



<b>A5</b>	Generate and Describe Sequences	<b>S2</b>	Theoretical Probability	<b>A4</b>	Plotting Vertical and Horizontal Lines	<b>A3</b>	Formulae & Substitution
<b>N8</b>	Add and Subtract Fractions	<b>G6</b>	Constructions with Compasses	<b>G5</b>	Reflection & Rotation	<b>R2</b>	Converting Metric Units
<b>R3</b>	Proportion Scaling	<b>N7</b>	Fraction, Decimal & Percentage Equivalence	<b>N6</b>	Factors, Multiples & Primes	<b>N5</b>	Rounding to Multiples



<b>N1</b>	Calculations with Decimals	<b>G1</b>	Measures of 2D Shapes	<b>G2</b>	Properties of 2D Shapes	<b>A2</b>	Forming and Solving Equations
<b>N2</b>	Calculations with Negatives	<b>A1</b>	Introducing Algebraic Notation	<b>S1</b>	Representing Categorical Data	<b>N4</b>	Use of a Calculator
<b>N3</b>	Order of Operations	<b>R1</b>	Ratio and Fractions	<b>G3</b>	Angle Facts	<b>G4</b>	Nets of 3D Shapes



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